

# Lexical alignment: IBM models 1 and 2

## MLE via EM for categorical distributions

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## Translation data

Let's assume we are confronted with a new language  
and luckily we managed to obtain some sentence-aligned data

the black dog		□ ⊗
the nice dog		□ ∪
the black cat		□ • ⊗
a dog chasing a cat		□ • < □

## Translation data

Let's assume we are confronted with a new language and luckily we managed to obtain some sentence-aligned data

the black dog		□ ⊗
the nice dog		□ ∪
the black cat		□ • ⊗
a dog chasing a cat		□ • ◁ □

Is there anything we could say about this language?

## Translation by analogy

the black dog		□ ⊗
the nice dog		□ ∪
the black cat		□ ⊙ ⊗
a dog chasing a cat		□ ⊙ ◁ □

A few hypotheses:

## Translation by analogy

the black dog		□ ⊗
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the black cat		□ ⊙ ⊗
a dog chasing a cat		□ ⊙ ◁ □

A few hypotheses:

- ▶ □  $\iff$  dog

## Translation by analogy

the black dog		$\square \circledast$
the nice dog		$\square \cup$
the black cat		$\square \cdot \circledast$
a dog chasing a cat		$\square \cdot \triangleleft \square$

A few hypotheses:

- ▶  $\square \iff \text{dog}$
- ▶  $\square \cdot \iff \text{cat}$

## Translation by analogy

the black dog		□ ⊛
the nice dog		□ ∪
the black cat		□ <sup>•</sup> ⊛
a dog chasing a cat		□ <sup>•</sup> ◁ □

A few hypotheses:

- ▶ □  $\iff$  dog
- ▶ □<sup>•</sup>  $\iff$  cat
- ▶ ⊛  $\iff$  black

## Translation by analogy

the black dog		□ ⊛
the nice dog		□ U
the black cat		◻ ⊛
a dog chasing a cat		◻ ◁ □

A few hypotheses:

- ▶ □  $\iff$  dog
- ▶ ◻  $\iff$  cat
- ▶ ⊛  $\iff$  black
- ▶ nouns seem to precede adjectives



## Translation by analogy

the black dog		□ ⊛
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the black cat		◻ ⊛
a dog chasing a cat		◻ ◀ □

A few hypotheses:

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- ▶ nouns seem to precede adjectives
- ▶ determiners are probably not expressed

## Translation by analogy

the black dog		□ *
the nice dog		□ U
the black cat		□* *
a dog chasing a cat		□* ◁ □

A few hypotheses:

- ▶ □  $\iff$  dog
- ▶ □\*  $\iff$  cat
- ▶ \*  $\iff$  black
- ▶ nouns seem to precede adjectives
- ▶ determiners are probably not expressed
- ▶ *chasing* may be expressed by ◁  
and perhaps this language is OVS

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the black cat		□ *
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A few hypotheses:

- ▶ □  $\iff$  dog
- ▶ □  $\iff$  cat
- ▶ \*  $\iff$  black
- ▶ nouns seem to precede adjectives
- ▶ determiners are probably not expressed
- ▶ *chasing* may be expressed by ◁  
and perhaps this language is OVS
- ▶ or perhaps *chasing* is realised by a verb with swapped arguments

# Probabilistic lexical alignment models

This lecture is about operationalising this intuition

- ▶ through a probabilistic learning algorithm
- ▶ for a non-probabilistic approach see for example [Lardilleux and Lepage, 2009]

# Content

Lexical alignment

Mixture models

IBM model 1

IBM model 2

Decoding

Remarks

## Word-to-word alignments

Imagine you are given a text

the black dog		el perro negro
the nice dog		el perro bonito
the black cat		el gato negro
a dog chasing a cat		un perro persiguiendo a un gato

## Word-to-word alignments

Now imagine the French words were replaced by placeholders

the black dog		$F_1$	$F_2$	$F_3$		
the nice dog		$F_1$	$F_2$	$F_3$		
the black cat		$F_1$	$F_2$	$F_3$		
a dog chasing a cat		$F_1$	$F_2$	$F_3$	$F_4$	$F_5$

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and suppose our task is to have a model explain the original data



## Word-to-word alignments

Now imagine the French words were replaced by placeholders

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the nice dog	$F_1$	$F_2$	$F_3$		
the black cat	$F_1$	$F_2$	$F_3$		
a dog chasing a cat	$F_1$	$F_2$	$F_3$	$F_4$	$F_5$

and suppose our task is to have a model explain the original data  
*by generating each French word from exactly one English word*

# Generative story

For each sentence pair independently,

1. observe an English sentence  $e_1, \dots, e_m$   
and a French sentence length  $n$
2. for each French word position  $j$  from 1 to  $n$ 
  - 2.1 select an English position  $a_j$
  - 2.2 conditioned on the English word  $e_{a_j}$ , generate  $f_j$

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We have introduced an **alignment**  
which is not directly visible in the data

# Data augmentation

Observations:

the black dog | el perro negro

Imagine data is made of pairs:  $(a_j, f_j)$  and  $e_{a_j} \rightarrow f_j$

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the black dog |  $(A_1, E_{A_1} \rightarrow F_1)$   $(A_2, E_{A_2} \rightarrow F_2)$   $(A_3, E_{A_3} \rightarrow F_3)$

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the black dog |  $(1, E_{A_1} \rightarrow F_1)$   $(A_2, E_{A_2} \rightarrow F_2)$   $(A_3, E_{A_3} \rightarrow F_3)$

# Data augmentation

Observations:

the black dog | el perro negro

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the black dog |  $(1, \text{the} \rightarrow \text{el}) (A_2, E_{A_2} \rightarrow F_2) (A_3, E_{A_3} \rightarrow F_3)$

# Data augmentation

Observations:

the black dog | el perro negro

Imagine data is made of pairs:  $(a_j, f_j)$  and  $e_{a_j} \rightarrow f_j$

the black dog | (1, the  $\rightarrow$  el) (3,  $E_{A_2} \rightarrow F_2$ ) ( $A_3, E_{A_3} \rightarrow F_3$ )



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Imagine data is made of pairs:  $(a_j, f_j)$  and  $e_{a_j} \rightarrow f_j$

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the black dog | (1, the  $\rightarrow$  el) (3, dog  $\rightarrow$  perro) (2, black  $\rightarrow$  negro)

the black dog | ( $A_1$ , the  $\rightarrow$  el) ( $A_1$ , the  $\rightarrow$  perro) ( $A_1$ , the  $\rightarrow$  negro)

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# Content

Lexical alignment

**Mixture models**

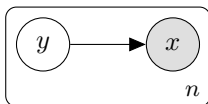
IBM model 1

IBM model 2

Decoding

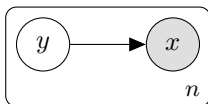
Remarks

## Mixture models: generative story



- ▶  $c$  mixture components
- ▶ each defines a distribution over the same data space  $\mathcal{X}$
- ▶ plus a distribution over components themselves

## Mixture models: generative story



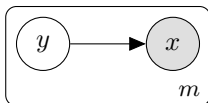
- ▶  $c$  mixture components
- ▶ each defines a distribution over the same data space  $\mathcal{X}$
- ▶ plus a distribution over components themselves

### Generative story

1. select a mixture component  $y \sim p(y)$
2. generate an observation from it  $x \sim p(x|y)$



## Mixture models: likelihood



Incomplete-data likelihood

$$p(x_1^m) = \prod_{i=1}^m p(x_i) \quad (1)$$

$$= \prod_{i=1}^m \sum_{y=1}^c \underbrace{p(x_i, y)}_{\text{complete-data likelihood}} \quad (2)$$

$$= \prod_{i=1}^m \sum_{y=1}^c p(y)p(x_i|y) \quad (3)$$

# Interpretation

## Missing data

- ▶ Let  $y$  take one of  $c$  mixture components
- ▶ Assume data consists of pairs  $(x, y)$
- ▶  $x$  is always observed
- ▶  $y$  is always missing

# Interpretation

## Missing data

- ▶ Let  $y$  take one of  $c$  mixture components
- ▶ Assume data consists of pairs  $(x, y)$
- ▶  $x$  is always observed
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Inference: posterior distribution over possible  $y$  for each  $x$

$$p(y|x) = \frac{p(y, x)}{\sum_{y'=1}^c p(y', x)} \quad (4)$$

$$= \frac{p(y)p(x|y)}{\sum_{y'=1}^c p(y')p(x|y')} \quad (5)$$

# Non-identifiability

Different parameter settings, same distribution

Suppose  $\mathcal{X} = \{a, b\}$  and  $c = 2$   
and let  $p(y = 1) = p(y = 2) = 0.5$

$y$	$x = a$	$x = b$
1	0.2	0.8
2	0.7	0.3
$p(x)$	0.45	0.55

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Problem for parameter estimation by hillclimbing

## Maximum likelihood estimation

Suppose a dataset  $\mathcal{D} = \{x^{(1)}, x^{(2)}, \dots, x^{(m)}\}$

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Likelihood of iid observations

$$p(\mathcal{D}) = \prod_{i=1}^m p_{\theta}(x^{(i)})$$



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the score function is

$$l(\theta) = \sum_{i=1}^m \log p_{\theta}(x^{(i)})$$

# Maximum likelihood estimation

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Likelihood of iid observations

$$p(\mathcal{D}) = \prod_{i=1}^m p_{\theta}(x^{(i)})$$

the score function is

$$l(\theta) = \sum_{i=1}^m \log p_{\theta}(x^{(i)})$$

then we choose

$$\theta^* = \arg \max_{\theta} l(\theta)$$

# MLE for categorical: estimation from fully observed data

Suppose we have **complete data**

$$\blacktriangleright \mathcal{D}_{\text{complete}} = \{(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})\}$$

# MLE for categorical: estimation from fully observed data

Suppose we have **complete data**

$$\blacktriangleright \mathcal{D}_{\text{complete}} = \{(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})\}$$

Then, for a **categorical distribution**

$$p(x|y) = \theta_{y,x}$$

and  $n(y, x | \mathcal{D}_{\text{complete}}) = \text{count of } (y, x) \text{ in } \mathcal{D}_{\text{complete}}$

MLE solution:

$$\theta_{y,x} = \frac{n(y, x | \mathcal{D}_{\text{complete}})}{\sum_{x'} n(y, x' | \mathcal{D}_{\text{complete}})}$$

# MLE for categorical: estimation from incomplete data

## Expectation-Maximisation algorithm [Dempster et al., 1977]

E-step:

- ▶ for every observation  $x$ , imagine that every possible latent assignment  $y$  happened with probability  $p_{\theta}(y|x)$

$$\mathcal{D}_{\text{completed}} = \{(x, y = 1), \dots, (x, y = c) : x \in \mathcal{D}\}$$

# MLE for categorical: estimation from incomplete data

**Expectation-Maximisation algorithm** [Dempster et al., 1977]

M-step:

- ▶ reestimate  $\theta$  as to climb the likelihood surface
- ▶ for categorical distributions  $p(x|y) = \theta_{y,x}$   
 $y$  and  $x$  are categorical  
 $0 \leq \theta_{y,x} \leq 1$  and  $\sum_{x \in X} \theta_{y,x} = 1$

$$\theta_{y,x} = \frac{\mathbb{E}[n(y \rightarrow x | \mathcal{D}_{\text{completed}})]}{\sum_{x'} \mathbb{E}[n(y \rightarrow x' | \mathcal{D}_{\text{completed}})]} \quad (6)$$

$$= \frac{\sum_{i=1}^m \sum_{y'} p(y'|x^{(i)}) \mathbf{1}_y(y') \mathbf{1}_x(x^{(i)})}{\sum_{i=1}^m \sum_{x'} \sum_{y'} p(y'|x^{(i)}) \mathbf{1}_y(y') \mathbf{1}_{x'}(x^{(i)})} \quad (7)$$

$$= \frac{\sum_{i=1}^m p(y|x^{(i)}) \mathbf{1}_x(x^{(i)})}{\sum_{i=1}^m \sum_{x'} p(y|x^{(i)}) \mathbf{1}_{x'}(x^{(i)})} \quad (8)$$

# Content

Lexical alignment

Mixture models

**IBM model 1**

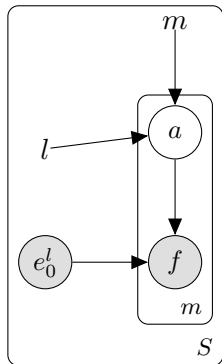
IBM model 2

Decoding

Remarks

# IBM1: a constrained mixture model

Constrained mixture model

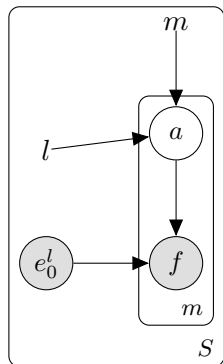




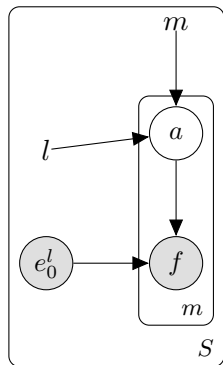
# IBM1: a constrained mixture model

## Constrained mixture model

- ▶ mixture components are English words



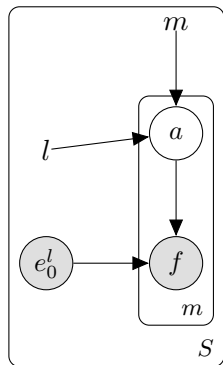
# IBM1: a constrained mixture model



## Constrained mixture model

- ▶ mixture components are English words
- ▶ but only English words that appear in the English sentence can be assigned

# IBM1: a constrained mixture model



## Constrained mixture model

- ▶ mixture components are English words
- ▶ but only English words that appear in the English sentence can be assigned
- ▶  $a_j$  acts as an indicator for the mixture component that generates French word  $f_j$
- ▶  $e_0$  is occupied by a special NULL component
- ▶  $j$  ranges over French words and  $i$  over English words

# Parameterisation

Alignment distribution: uniform

$$p(a|l, m) = \frac{1}{l+1} \quad (9)$$

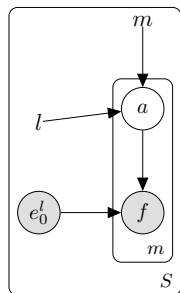
Lexical distribution: categorical

$$p(f|e) = \text{Cat}(f|\theta_e) \quad (10)$$

- ▶ where  $\theta_e \in \mathbb{R}^{v_F}$
- ▶  $0 \leq \theta_{e,f} \leq 1$
- ▶  $\sum_f \theta_{e,f} = 1$

# IBM1: incomplete-data likelihood

## Incomplete-data likelihood



$$p(f_1^m | e_0^l) = \sum_{a_1=0}^l \cdots \sum_{a_m=0}^l p(f_1^m, a_1^m | e_{a_j}) \quad (11)$$

$$= \sum_{a_1=0}^l \cdots \sum_{a_m=0}^l \prod_{j=1}^n p(a_j | l, m) p(f_j | e_{a_j}) \quad (12)$$

$$= \prod_{j=1}^n \sum_{a_j=0}^l p(a_j | l, m) p(f_j | e_{a_j}) \quad (13)$$

## IBM1: posterior

Posterior

$$p(a_1^m | f_1^m, e_0^l) = \frac{p(f_1^m, a_1^m | e_0^l)}{p(f_1^m | e_0^l)} \quad (14)$$

Factorised

$$p(a_j | f_1^m, e_0^l) = \frac{p(a_j | l, m) p(f_j | e_{a_j})}{\sum_{i=0}^l p(i | l, m) p(f_j | e_i)} \quad (15)$$

## MLE via EM

E-step:

$$\mathbb{E}[n(\mathbf{e} \rightarrow \mathbf{f} | a_1^m)] = \sum_{a_1=0}^l \cdots \sum_{a_m=0}^l p(a_1^m | f_1^m, e_0^l) n(\mathbf{e} \rightarrow \mathbf{f} | A_1^m) \quad (16)$$

$$= \sum_{a_1=0}^l \cdots \sum_{a_m=0}^l \prod_{j=1}^m p(a_j | f_1^m, e_0^l) \mathbf{1}_{\mathbf{e}}(e_{a_j}) \mathbf{1}_{\mathbf{f}}(f_j) \quad (17)$$

$$= \prod_{j=1}^m \sum_{i=0}^l p(a_j = i | f_1^m, e_0^l) \mathbf{1}_{\mathbf{e}}(e_i) \mathbf{1}_{\mathbf{f}}(f_j) \quad (18)$$

M-step:

$$\theta_{e,f} = \frac{\mathbb{E}[n(\mathbf{e} \rightarrow \mathbf{f} | a_1^m)]}{\sum_{f'} \mathbb{E}[n(\mathbf{e} \rightarrow \mathbf{f}' | a_1^m)]} \quad (19)$$

# EM algorithm

Repeat until convergence to a local optimum

1. For each sentence pair
  - 1.1 compute posterior per alignment link
  - 1.2 accumulate fractional counts
2. Normalise counts for each English word



# Content

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IBM model 1

**IBM model 2**

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# Alignment distribution

## Positional distribution

$$p(a_j|l, m) = \text{Cat}(a|\lambda_{j,l,m})$$

- ▶ one distribution for each tuple  $(j, l, m)$
- ▶ support must include length of longest English sentence
- ▶ extremely over-parameterised!

# Alignment distribution

## Positional distribution

$$p(a_j|l, m) = \text{Cat}(a|\lambda_{j,l,m})$$

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- ▶ support must include length of longest English sentence
- ▶ extremely over-parameterised!

## Jump distribution

[Vogel et al., 1996]

- ▶ define a jump function  $\delta(a_j, j, l, m) = a_j - \lfloor j \frac{l}{m} \rfloor$
- ▶  $p(a_j|l, m) = \text{Cat}(\Delta|\lambda)$
- ▶  $\Delta$  takes values from  $-\text{longest}$  to  $+\text{longest}$

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**Decoding**

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# Decoding

- ▶ Pick the alignment that has the highest posterior probability.
- ▶ Assumption conditional independence of alignment links  
Maximising the probability of an alignment factorises over individual alignment links.
- ▶  $\mathit{arg\ max} p(a_1^m \mid f_1^m, e_0^l)$

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Lexical alignment

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## Note on terminology: source/target vs French/English

From an alignment model perspective all that matters is

- ▶ we condition on one language and generate the other
- ▶ in IBM models terminology, we condition on *English* and generate *French*

From a noisy channel perspective, where we want to translate a *source* sentence  $f_1^n$  into some *target* sentence  $e_1^l$

- ▶ Bayes rule decomposes  $p(e_1^l | f_1^n) \propto p(f_1^n | e_1^l) p(e_1^l)$
- ▶ train  $p(e_1^l)$  and  $p(f_1^n | e_1^l)$  independently
- ▶ **language model:**  $p(e_1^l)$
- ▶ **alignment model:**  $p(f_1^n | e_1^l)$
- ▶ note that the alignment model conditions on the target sentence (English) and generates the source sentence (French)

## Limitations of IBM1-2

- ▶ too strong independence assumptions
- ▶ categorical parameterisation suffers from data sparsity
- ▶ EM suffers from local optima



# Extensions

Fertility, distortion, and concepts [Brown et al., 1993]

Dirichlet priors and posterior inference [Mermer and Saraclar, 2011]

- ▶ + no NULL words [Schulz et al., 2016]
- ▶ + HMM and efficient sampler [Schulz and Aziz, 2016]

Log-linear distortion parameters and variational Bayes  
[Dyer et al., 2013]

First-order dependency (HMM) [Vogel et al., 1996]

- ▶ E-step requires dynamic programming  
[Baum and Petrie, 1966]

## References I

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