Lexical alignment: feature-rich models

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Position parameterisation $L^2 \times M^2$ Jump distribution [Vogel et al., 1996]

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 A jump quantifies a notion of mismatch in linear order between French and English Leads to a very small number of parameters, 2 × L

IBM 2 EM

0 1: $N \leftarrow$ number of sentence pairs 2: $I \leftarrow$ number of iterations 3: $\lambda \leftarrow$ lexical parameters 4: $\gamma \leftarrow \text{alignment parameters}$ 5: 6: for $i \in [1, ..., I]$ do E step: 7: $n(\lambda_{e,f}) \leftarrow 0$ $\forall (\mathsf{e},\mathsf{f}) \in V_E imes V_F$ 8: $n(\gamma_r) \leftarrow 0$ $\forall x \in [-L, L]$ 9: for $s \in [1, \ldots, N]$ do 10: for $j \in [1, \ldots, m^{(s)}]$ do 11: for $i \in [0, ..., l^{(s)}]$ do 12: $x \leftarrow \text{jump}(i, j, l^{(s)}, m^{(s)})$ 13: $\frac{\lambda_{e_i,f_j} \times \gamma_x}{n(\lambda_{e_i,f_j}) \leftarrow n(\lambda_{e_i,f_j}) + \frac{\lambda_{e_i,f_j} \times \gamma_x}{\sum_{k=0}^l \lambda_{e_k,f_j} \times \gamma_{ijum(k,i,l^{(s)},m^{(s)})}}$ 14: $n(\gamma_x) \leftarrow n(\gamma_x) + \frac{\lambda_{e_i, f_j} \times \gamma_{jump(i, j, l, m)}}{\sum_{k=1}^l \lambda_{e_k, f_j} \times \gamma_{iump(k, j, l^{(s)}, m^{(s)})}}$ 15: end for 16:17:end for end for 18: 19: 20: M step:
$$\begin{split} \lambda_{\mathbf{e},\mathbf{f}} &\leftarrow \frac{n(\lambda_{\mathbf{e},f})}{\sum_{t' \in V_F} n(\lambda_{\mathbf{e},t'})} \qquad \forall (\mathbf{e},\mathbf{f}) \in V_E \times V_F \\ \gamma_x &\leftarrow \frac{n(\gamma_x)}{\sum_{x' \in [-L,L]} n(\gamma_{x'})} \qquad \forall x \in [-L,L] \end{split}$$
21:22:23: end for

3/31

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- In practice, one usually starts from uniform parameters. [Toutanova and Galley, 2011] show better initialisations

IBM 2

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- In practice, one initialises the component distributions of IBM2 (i.e. its translation parameters) with IBM1 estimates.
- The alignment distributions are initialised uniformly. Notice we first have to train IBM1 before proceeding to IBM2

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Parameterisation

 categorical events are unrelated prefixes/suffixes: normal, normally, abnormally, ... verb inflections: comer, comi, comia, comio, ... gender/number: gato, gatos, gata, gatas, ...

CPD: condition $c \in C$, outcome $o \in O$, and $\theta_c \in \mathbb{R}^{|O|}$

$$p(o|c) = \operatorname{Cat}(\theta_c) \tag{1}$$

$$\blacktriangleright p(o|c) = \theta_{c,o}$$

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• $O(|j| \times |i|)$ parameters

Probability tables

p(f|e)

English \downarrow	$FRENCH \rightarrow$				
	anormal	normal	normalmente		
abnormal	0.7	0.1	0.01		
normal	0.01	0.6	0.2		
normally	0.001	0.25	0.65		

- grows with size of vocabularies
- no parameter sharing

Logistic CPDs

CPD: condition $c \in \mathcal{C}$ and outcome $o \in \mathcal{O}$

$$p(o|c) = \frac{\exp(w^{\top}h(c,o))}{\sum_{o'}\exp(w^{\top}h(c,o'))}$$
(2)

- $w \in \mathbb{R}^d$ is a weight vector
- $h: \mathcal{C} \times \mathcal{O} \rightarrow R^d$ is a feature function
- d parameters
- ▶ computing CPD requires $O(|j| \times |i| \times d)$ operations

CPDs as functions

 $h: \mathcal{E} \times \mathcal{F} \to R^d$

Events \downarrow		$Features \rightarrow$				
English	French	normal	normal-	-normal	ab-	-ly
	FRENCH	normal	normal-	<u>-normal</u>	a-	-mente
abnormal	anormal	0	0	1	1	0
	normal	0	0	1	0	0
	<i>normal</i> mente	0	1	0	0	0
normal	a <u>normal</u>	0	0	1	0	0
	normal	1	0	0	0	0
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normally	a <u>normal</u>	0	0	1	0	0
	normal	0	1	0	0	0
	normalmente	0	1	0	0	1
Weights \rightarrow		1.5	0.3	0.3	0.8	1.1

- computation still grows with size of vocabularies
- but far less parameters to estimate

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 Something about the context that will be useful in predicting
- Enhancing models with features that capture the dependencies between different morphologically inflected word forms. The standard parameterisation using categorical distributions is limited with respect to the features it can capture

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Berg-Kirkpatrick et al. [2010]

Lexical distribution in IBM model 1

$$p(f|e) = \frac{\exp(w_{\mathsf{lex}}^{\top} h_{\mathsf{lex}}(e, f))}{\sum_{f'} \exp(w_{\mathsf{lex}}^{\top} h_{\mathsf{lex}}(e, f'))}$$
(3)

Features

- $f \in V_F$ is a French word (decision), $e \in V_E$ is an English word (conditioning context), $w \in R^d$ is the parameter vector, and $h: V_F V_E \to R^d$ is a feature vector function.
- prefixes/suffixes
- character n-grams
- POS tags

Extension: lexicalised jump distribution

$$p(\delta|e) = \frac{\exp(w_{\mathsf{dist}}^{\top} h_{\mathsf{dist}}(e, \delta))}{\sum_{\delta'} \exp(w_{\mathsf{dist}}^{\top} h_{\mathsf{dist}}(e, \delta'))}$$
(4)

Features

- POS tags
- suffixes/prefixes
- Iemma
- jump values
- m, n, j, i (values used to compute jump)

Feature name	Description
word	Whole lexical entry
prefix	Prefix of specified length
suffix	Suffix of specified length
category	Boolean: checks if lexical entry contains digit(s)

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- ▶ and e_{t-1} = eat is also compatible (in the context cows eat hay).

farmers eat	$\begin{array}{l} \text{steak} \rightarrow \\ \text{hay} \rightarrow \end{array}$		cows eat	$\begin{array}{l} \text{steak} \rightarrow \\ \text{hay} \rightarrow \end{array}$	
farmers grow	$\begin{array}{l} \text{steak} \rightarrow \\ \text{hay} \rightarrow \end{array}$	low high	cows grow	$\begin{array}{l} \text{steak} \rightarrow \\ \text{hay} \rightarrow \end{array}$	

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- Learning using these combination features, e.g. neural networks

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- We can use a linear combination y = Wx + b
- Or a multi-layer perceptron:

$$h = step(W_x h_x + b_h)$$

$$y = w_{hy}h + b_y.$$
(5)

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- \blacktriangleright Calculation of the hidden layer , which takes in input x and outputs a vector of hidden variables h

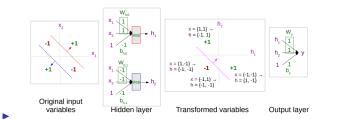
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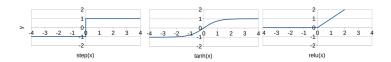
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- e.g. squared-error loss, common in regression problems which measures the difference between the calculated value y and correct value y*: l(y*, y) = (y* - y)²
- however the step() function is not very derivative friendly
- We can use non-linear functions, hyperbolic tangent (tanh) function



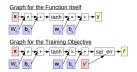
▶ We perform the full calculation of the loss function:

$$\begin{aligned} \boldsymbol{h}' &= W_{xh}\boldsymbol{x} + \boldsymbol{b}_h \\ \boldsymbol{h} &= \tanh(\boldsymbol{h}') \\ \boldsymbol{y} &= \boldsymbol{w}_{hy}\boldsymbol{h} + \boldsymbol{b}_y \\ \boldsymbol{\ell} &= (y^* - y)^2. \end{aligned}$$

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We use chain rule of derivatives for each set of parameters:

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- ▶ induce features (word-level, char-level, *n*-gram level)
- pre-trained embeddings

• $f_{\theta}(e) = \operatorname{softmax}(W_t H_E(e) + b_t)$ note that the softmax is necessary to make t_{θ} produce valid parameters for the categorical distribution $W_t \in \mathbb{R}^{|V_F| \times d_h}$ and $b_t \in \mathbb{R}^{|V_F|}$

▶ $h_E(e)$ is defined below with $W_{h_E} \in \mathbb{R}^{d_h \times d_e}$ and $b_{h_E} \in \mathbb{R}^{d_h}$ $h_E(e) = \tanh(\underbrace{W_{h_E}r_E(e) + b_{h_E}}_{\text{affine}})$

elementwise nonlinearity

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h_E(e) is defined below with *W_{hE}* ∈ ℝ<sup>d_h×d_e and *b_{hE}* ∈ ℝ^{d_h}
 h_E(e) = tanh(<u>W_{hE}r_E(e) + b_{hE})</u> affine elementwise nonlinearity

 r_E(e) = W_{r_E}v_E(e) is a word embedding of *e* with *W_{r_E}* ∈ ℝ<sup>d_e×|V_E|

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θ = {W_t, b_t, W_{hE}, b_{hE}, W_{rE}}
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▶ $h_E(e)$ is defined below with $W_{h_E} \in \mathbb{R}^{d_h \times d_e}$ and $b_{h_E} \in \mathbb{R}^{d_h}$ $h_E(e) = \tanh(\underbrace{W_{h_E}r_E(e) + b_{h_E}}_{\text{affine}})$ elementwise nonlinearity

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- ▶ $v_E(e) \in \{0,1\}^{v_E}$ is a one-hot encoding of e, thus $\sum_i v_E(e)_i = 1$

•
$$\theta = \{W_t, b_t, W_{h_E}, b_{h_E}, W_{r_E}\}$$

Other architectures are also possible, one can use different parameterisations that may use more or less parameters. For example, with a CNN one could make this function sensitive to characters in the words, something along these lines could also be done with RNNs.

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 This is a gradient-based procedure which chooses θ so that the gradient of our objective with respect to θ is zero.
- IBM1 would be convex with standard tabular CPDs, but FFNNs with 1 non-linear hidden layer (or more) make it non-convex.

- We can use maximum likelihood estimation (MLE) to choose the parameters of our deterministic function f_{θ} .
- We know at least one general (convex) optimisation algorithm, i.e. gradient ascent.
 This is a gradient-based procedure which chooses θ so that the gradient of our objective with respect to θ is zero.
- IBM1 would be convex with standard tabular CPDs, but FFNNs with 1 non-linear hidden layer (or more) make it non-convex.
- Nowadays, we have tools that can perform automatic differentiation for us.
 If our functions are differentiable, we can get gradients for them.

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- Let us then express the log-likelihood (which is the objective we maximise in MLE) of a single sentence pair as a function of our free parameters:

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► Note that in fact our log-likelihood is a sum of independent terms L_j(θ|e₀^m, f_j), thus we can characterise the contribution of each French word in each sentence pair as

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- NN toolkits implement gradient-based optimisation for us.
- To get a loss, we simply negate our objective.
 You will find a lot of material that mentions some categorical cross-entropy loss.

$$l(\theta) = -\sum_{(e_0^m, f_1^l)} p_{\star}(f_1^l | e_0^m) \log p_{\theta}(f_1^m | e_0^l) \\ \approx -\frac{1}{S} \log p_{\theta}(f_1^l | e_0^m)$$
(8)

► With SGD we sample a subset S of the training data and compute a loss for that sample.

- With SGD we sample a subset S of the training data and compute a loss for that sample.
- We then use automatic differentiation to obtain a gradient ∇_θ↓(θ|S). This gradient is used to update our deterministic parameters θ.

$$\theta^{(t+1)} = \theta^{(t)} - \delta_t \nabla_{\theta^{(t)}} l(\theta^{(t)} | \mathcal{S})$$
(9)

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